

Signature Verification based on the Control Theory of Skilled Movements

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Abstract

Dynamic signature verification based on temporal features are more precise than the static methods because in addition to position information of the drawing pattern, it uses local and global features extracted from velocity, acceleration, pressure and pen angle signals, while static methods only use image information. In this study, we segmented the signature patterns using the basic role of velocity in the control process of skilled movements and then the function features were extracted. In order to signal the matching evaluation, we applied five generalized functions and five weighting strategies for score level fusion. The results showed that the correlation criterion had the minimum error. The experiments on the database, consisting of persons of Persian, Chinese and English, showed that the skilled forgeries obtained an equal error rate (EER) of 0.87% and 1.24% for the user and universal thresholds, respectively.

Keywords: Dynamic signature verification; Dynamic time warping; Model of delta log-normal; Motor control; Segmenting

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EER

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$(v_x(t), v_y(t))$

$(x(t), y(t))$

:

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$$h_{ij}(t)$$

(CNS)

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$$A(t; t_0, \mu, \sigma) = \frac{1}{\sigma\sqrt{2\pi}(t-t_0)} \exp\left[-\frac{\ln(t-t_0-\mu)^2}{2\sigma^2}\right] \quad () \quad . []$$

$$V(t) = D_1 A(t; t_0, \mu_1, \sigma_1) - D_2 A(t; t_0, \mu_2, \sigma_2) \quad ()$$

$$\sigma_i, \mu_i$$

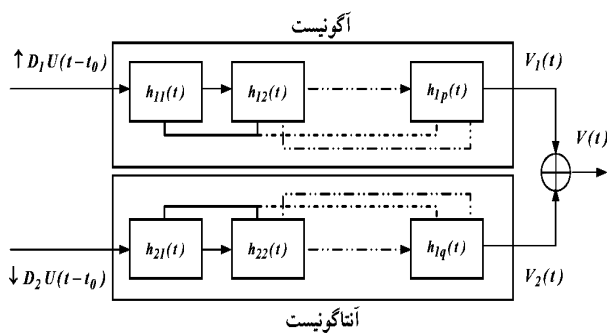
$$D_i$$

$$t_0$$

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⁵ Central Nervous System
⁹ Antagonist

⁶ Plamondon
¹⁰ Stroke

⁷ Delta Log-Normal

⁸ Agonist

$$V_{\theta(i)}(t) = C_{0(i)} \times V_{(i)}(t) \quad ()$$

$$\begin{aligned} &: \theta_0 & & : P_0 \\ & & & : C_0 \end{aligned}$$

$$V(t) = D_1 \mathcal{A}(t; t_0, \mu_1, \sigma_1) - D_2 \mathcal{A}(t; t_0, \mu_2, \sigma_2) \quad ()$$

$$\angle V(t) = \theta(t) = \theta_0 + C_0 \int_{t_0}^t |\vec{V}(\tau)| d\tau \quad ()$$

$$\omega(t) = \frac{d\theta(t)}{dt} = C_0 |\vec{V}(t)| \quad ()$$

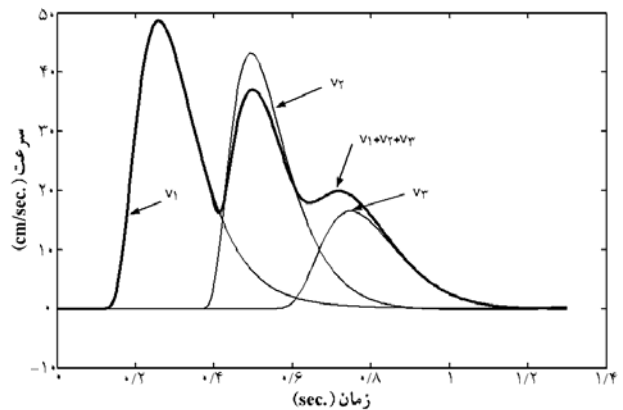
$$C_{0(i)} \approx \frac{V_{\theta}(t_{max_v(i)})}{V(t_{max_v(i)})} \quad ()$$

$$\theta_{0(i)} \approx \theta(t_{max_v(i)}) - C_{0(i)} \int_{t_0(i)}^{t_{max_v(i)}} V_{(i)}(t) dt \quad ()$$

$$V(t) = \left| \sum_{i=1}^n \vec{V}_{(i)}(t) \right| \quad ()$$

$$\theta(t) = \arctan \left[\frac{\sum_{i=1}^n \vec{V}_{(i)}(t) \cdot \sin(\theta_{(i)}(t))}{\sum_{i=1}^n \vec{V}_{(i)}(t) \cdot \cos(\theta_{(i)}(t))} \right] \quad ()$$

$$[t_0, P_0, \theta_0, C_0, D_{1,2}, \mu_{1,2}, \sigma_{1,2}]$$



(x, y)

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θ_0

HZ

$$S_{N_i}(t) = \frac{S_i(t) - \mu_i}{\sigma_i}$$

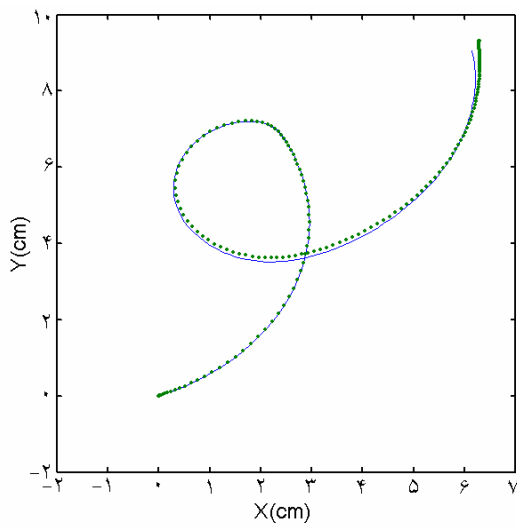
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σ_i, μ_i

PRD = % /



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¹² Simple Forgeries

¹³ Skilled Forgeries

¹⁴ Wacom

¹⁵ Graphier

¹⁶ Levenberg-Marquardt

IDDTW DTW EPW
 % EPW
 EPM .[]

$$PRD = \sqrt{\frac{\sum_{t_0}^{t_n} (v(t) - \hat{v}(t))^2}{\sum_{t_0}^{t_n} v(t)^2}} \quad ()$$

$\hat{v}(t)$

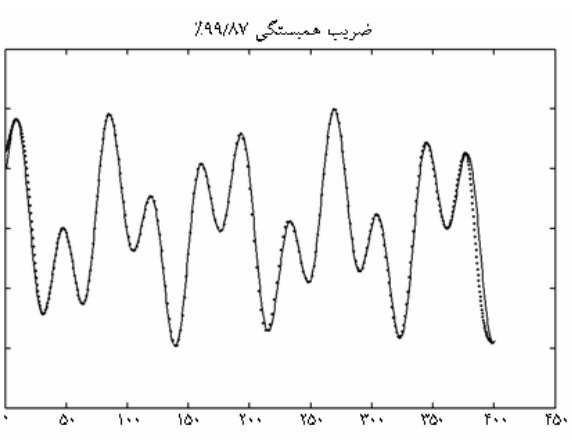
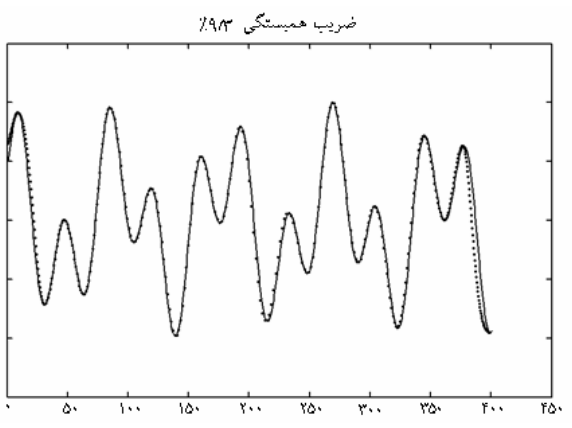
:DTW

(X, Y, [X, Y]) :

$$v = \sqrt{v_x^2 + v_y^2} \quad (v_x, v_y, [v_x, v_y])$$

($\theta, \cos(\theta), \sin(\theta)$)
 (v, θ)

EPW
 EPW



(:
 (...) :

(DTW)
 [] DTW
 DTW
 .[]
 EPW IDDTW
 .[]

¹⁷ Dynamic Time Warping

¹⁸ Iterative Deeping Dynamic Time Warping

¹⁹ Extreme Points Warping

m : n
 $P = p_{ij} \quad i = 1, 2, \dots, n / j = 1, 2, \dots, m$
 $Q = q_{ij} \quad i = 1, 2, \dots, n / j = 1, 2, \dots, m$

$$D(P, Q) = \sqrt{\frac{\sum_{j=1}^m \sum_{i=1}^n (p_{ij} - q_{ij})^2}{\sum_{j=1}^m \left[\sum_{i=1}^n p_{ij}^2 + \sum_{i=1}^n q_{ij}^2 \right]}}$$

$$D(P, Q) = \frac{\sum_{j=1}^m \sum_{i=1}^n |p_{ij} - q_{ij}|}{\sum_{j=1}^m \left[\sum_{i=1}^n |p_{ij}| + \sum_{i=1}^n |q_{ij}| \right]}$$

$$D(P, Q) = \frac{1}{n \times m} \sum_{j=1}^m \sum_{i=1}^n \frac{|p_{ij} - q_{ij}|}{|p_{ij}| + |q_{ij}|}$$

$$D(P, Q) = 1 - \frac{\sum_{j=1}^m \sum_{i=1}^n p_{ij} q_{ij}}{\sqrt{\sum_{j=1}^m \left[\sum_{i=1}^n p_{ij}^2 \cdot \sum_{i=1}^n q_{ij}^2 \right]}}$$

$$D(P, Q) = 1 - \frac{\sum_{j=1}^m \sum_{i=1}^n (p_{ij} - \mu_{p_j})(q_{ij} - \mu_{q_j})}{\sqrt{\sum_{j=1}^m \left[\sum_{i=1}^n (p_{ij} - \mu_{p_j})^2 \cdot \sum_{i=1}^n (q_{ij} - \mu_{q_j})^2 \right]}}$$

μ_{q_j}, μ_{p_j}
) DTW
 () EPW ()
)
 (

(P, Q)
 : EPW DTW

$$D_s(\text{stroke}) = \sqrt{\sum_{f=1}^F \left(\frac{D_{s_f}(P, Q) - \mu_{s_f}(P, Q)}{\sigma_{s_f}(P, Q)} \right)^2}$$

$D_{s_f}(P, Q)$ F
 $\sigma_{s_f}(P, Q)$ $\mu_{s_f}(P, Q)$ s

$$D_{signature} = \sqrt{\frac{\sum_{s=1}^S D_s(\text{stroke})^2}{S}}$$

S

²⁰ Euclidian Distance ²¹ City Block Distance ²² Canberra Distance ²³ Cosine Distance
²⁴ Correlation Distance

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$$D_{Normalized} = \exp\left(-\frac{D_{signature}}{k \cdot \text{Max}(D_{signature})}\right) \quad ()$$

(1 ≤ k ≤ 2) K

EER (EER)

(FAR)

(FRR)

EER %

Distances : d_1, d_2, \dots, d_k
 Weights : w_1, w_2, \dots, w_k
 Condition : $w_1 + w_2 + \dots + w_k = 1$ ()
 $k = 5$

Max($D_{signature}$)

EER

$$D_{Total} = w_1 d_1 + w_2 d_2 + \dots + w_k d_k$$

EER

$$d_i = \max(d_1, d_2, \dots, d_k) \Rightarrow \begin{cases} w_i = 1 \\ w_j = 0 \end{cases} \quad j \neq i \quad ()$$

%

$$w_1 = w_2 = \dots = w_k = \frac{1}{k} \quad ()$$

EER

$$eer_1 < eer_2 < \dots < eer_k$$

$$w_{k-i+1} = \frac{eer_i}{\sum_{j=1}^k eer_j} \quad ()$$

$$w_i = \frac{\left(\sum_{j=1}^k eer_j\right) - eer_i}{(k-1) \sum_{j=1}^k eer_j} \quad ()$$

EER

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	/	/	/	/	

²⁵ Equal Error Rate

²⁶ False Acceptance Rate

²⁷ False Rejection Rate

EER

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	/	/	/	/	

$$w_i = \frac{w_i^2(\text{linear } 1)}{\sum_{j=1}^k w_j^2(\text{linear } 1)} \quad ()$$

μ_0

$$\frac{\text{Mean}(\sigma(EER_{\text{signal}_{i=1:N}}))}{i} = \mu(EER_{\text{signal}_i})$$

EER

EER

i

EER

EER

$$\mu(EER_{\text{signal}_i})$$

N

$$\sigma(EER_{\text{signal}_{i=1:N}})$$

t

EER

$$\sigma(EER_{\text{signal}_{i=1:N}})$$

EER

$$\text{Mean}(\sigma(EER_{\text{signal}_{i=1:N}}))$$

EER

$$\frac{1}{C_i}$$

EER

$$t = \frac{|\mu_1 - \mu_2|}{\sqrt{\frac{\sigma_1^2}{N_1} + \frac{\sigma_2^2}{N_2}}} \quad ()$$

N_1, N_2

$$C_i$$

EER

$$C_i = \frac{\mu(EER_{\text{signal}_i})}{\text{Mean}(\sigma(EER_{\text{signal}_{i=1:N}}))} \quad \mu \leq \mu_0 \quad ()$$

()

()

EPM

DTW

()

C_i

()
 $[v, \theta]$ $[x, y]$ $[v_x, v_y]$

EER

%

$\sin(\theta)$ $\cos(\theta)$

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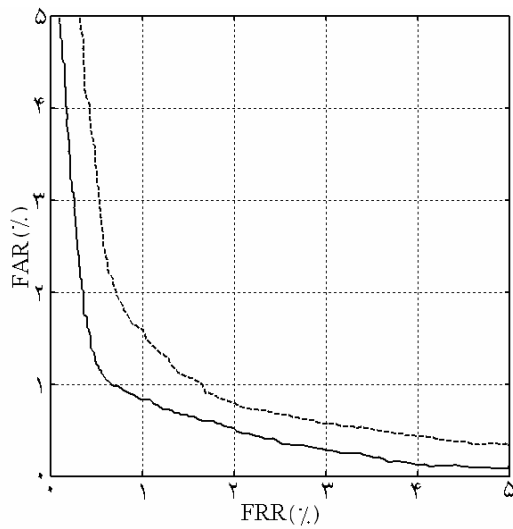
FAR

FRR

EER(%) :

/	/	
/	/	

(\times +)



(...) ()

				DTW $[v_x, v_y]$
				DTW $[v, \cos(\theta)]$
				EPM $v_y: y$
				DTW $[v, \sin(\theta)]$
				DTW $[v, \theta]$
				DTW $[X, Y]$
				EPM $v_x: x$
				EPM $\cos(\theta)$
				EPM v
				EPM Y
				EPM $\sin(\theta)$
				EPM θ
				EPM X

SVC2004

()
% EER

. [] % / EER

[V_x V_y] [X, Y]

[V, Sin(θ)] [V, Cos(θ)] [V, θ]

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% / EER

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